## ECE 101 Exploring Electrical Engineering

- Circuits 2
- Resistor
- Series and parallel connection of resistors
- Voltage Dividers
- Voltage \& Current Sources


## Resistor

- A resistor is a passive electronic component that obeys Ohm's Law. It has resistance $R$.
- SI Unit: ohm ( $\Omega$ )
- Symbol: - W-
- I-V relationship: $\quad v(t)=\operatorname{Ri}(t)$


$$
i(t)=\frac{1}{R} v(t)
$$



| Black | 0 | 0 | 0 | $1 \Omega$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Brown | 1 | 1 | 1 | $10 \Omega$ | $\pm 1 \%$ | (F) |
| Red | 2 | 2 | 2 | 1008 | $\pm 2 \%$ | (G) |
| Orange | 3 | 3 | 3 | $1 \mathrm{~K} \Omega$ |  |  |
| Yellow | 4 | 4 | 4 | $10 \mathrm{~K} \Omega$ |  |  |
| Green | 5 | 5 | 5 | $100 \mathrm{~K} \Omega$ | $\pm 0.5 \%$ | (D) |
| Blue | 6 | 6 | 6 | $1 \mathrm{M} \Omega$ | $\pm 0.25 \%$ | (C) |
| Violet | 7 | 7 | 7 | $10 \mathrm{M} \Omega$ | $\pm 0.10 \%$ | (B) |
| Grey | 8 | 8 | 8 |  | $\pm 0.05 \%$ |  |
| White | 9 | 9 | 9 |  |  |  |
| Gold |  |  |  | 0.1 | $\pm 5 \%$ | (J) |
| Silver |  |  |  | 0.01 | $\pm 10 \%$ | (K) |
| $\longrightarrow$ |  |  |  |  |  |  |



## Resistors Connected in Series (end-to-end)

- If $N$ resistors are connected in series, with the $i$-th resistor having a resistance $R_{i}$, then the equivalent resistance $R_{\text {eq }}$ is:


$$
\begin{gathered}
R_{\mathrm{eq}}=R_{1}+R_{2} \\
\longrightarrow \mathrm{~W}
\end{gathered}
$$



$$
\Rightarrow \overbrace{\text { eq }}=R_{1}+R_{2}+R_{3}
$$

$$
R_{\mathrm{eq}}=\sum_{i=1}^{N} R_{i}
$$

Properties of Series Resistances (DC):


- The amount of current $I_{\text {in }}$ entering one end of a series circuit is equal to the amount of current $I_{\text {out }}$ leaving the other end.
- The current is the same through each resistor in the series and is equal to $I_{\text {in }}$.

$$
I_{\mathrm{in}}=I_{\mathrm{out}}=I_{1}=I_{2}=I_{3}
$$

- The amount of voltage drop across each resistor in a series circuit is given by Ohm's Law.

$$
\begin{aligned}
& I \rightarrow \underbrace{R_{V}}_{+} \underbrace{R_{1}}_{V_{1}} \underbrace{R_{2}}_{V_{2}} \underbrace{R_{3}}_{V_{V_{3}}^{(2)}} \rightarrow I \\
& V_{1}=I R_{1}, V_{2}=I R_{2}, V_{3}=I R_{3}
\end{aligned}
$$

- By convention, the resistor terminal that the current enters is labeled " + ", and the terminal the current exits is labeled "-".
- KVL: total voltage drop = sum of individual drops (watch out for sign!)


## Example:


a) Calculate the current $I$ that flows through the resistors.
b) Find the voltage drop across the $6 \Omega$ resistor.

Solution:
a) Approach - Use Ohm's law: $\quad I=\frac{V_{A B}}{R_{e q}}$

Calculate the equivalent resistance: $R_{\mathrm{eq}}=(2+6+3) \Omega=11 \Omega$
Calculate the current: $I=\frac{3 \mathrm{~V}}{11 \Omega} \approx \underline{\underline{0.273 \mathrm{~A}}}$
b) Use Ohm's law again: $V_{6}=I R_{6}=(0.273 \mathrm{~A})(6 \Omega) \approx 1.64 \mathrm{~V}$

## Example:

- 100 V Source, 5 and 20 ohm resistors in series; find $R_{s}, I, P, V_{1}, V_{2}$
- 100 V Source, 5 and 20 ohm resistors in parallel; find $R_{p}, I, P, I_{1}, I_{2}$


## Resistors Connected in Parallel (side-by-side)

- If $N$ resistors are in parallel, with the $i$-th resistor having a resistance $R_{i}$, then the equivalent resistance is:

$$
\begin{aligned}
& R_{\mathrm{eq}}=\left(\sum_{i=1}^{N} \frac{1}{R_{i}}\right)^{-1} \longmapsto \\
& R_{1} \sum_{R_{2}} R_{2} \Rightarrow R_{\mathrm{eq}}=\left(\frac{1}{R_{1}}+\frac{1}{R_{2}}\right)^{-1}=\frac{R_{1} R_{2}}{R_{1}+R_{2}} \\
& R_{1} R_{2} R_{3} \Rightarrow R_{\mathrm{eq}}=\left(\frac{1}{R_{1}}+\frac{1}{R_{2}}+\frac{1}{R_{3}}\right)^{-1}
\end{aligned}
$$

Properties of Parallel Resistances (DC):


- The amount of current $I_{\text {in }}$ entering one end of a parallel circuit is equal to the amount of current $I_{\text {out }}$ leaving the other end: $I_{\text {in }}=I_{\text {out }}$
- For parallel resistors, the voltage drop across each resistor is the same: $V_{1}=V_{2}=V_{3}$
- KCL: $\Sigma$ (sum) of currents entering a node $=\Sigma$ (sum) of currents leaving a node


## Example:


a) Find the current $I_{\mathrm{x}}$ through the $2 \Omega$ resistor.
b) What is the power dissipated by the $3 \Omega$ resistor?

Assume 3 significant figures.

## Solution:

a) Approach - Use Ohm's law: $V_{A B}=I R_{e q}$

Calculate the equivalent resistance: $R_{\text {eq }}=\left(\frac{1}{2}+\frac{1}{6}+\frac{1}{3}\right)^{-1} \Omega=1 \Omega$
Calculate the voltage drop: $V_{A B}=(4 \mathrm{~A})(1 \Omega)=4 \mathrm{~V}$
Find the current: $I_{\mathrm{x}}=\frac{V_{A B}}{2 \Omega}=\underline{\underline{2.00 \mathrm{~A}}}$
b) Use power equation: $P=\frac{V_{A B}^{2}}{3 \Omega} \approx 5.33 \mathrm{~W}$

## Voltage Divider



$$
\begin{aligned}
& V_{1}=\frac{R_{1}}{R_{1}+R_{2}} V_{0} \\
& V_{2}=\frac{R_{2}}{R_{1}+R_{2}} V_{0}
\end{aligned}
$$

Voltage Divider

## Example:



What is the voltage drop across $R_{a}$ ?
$V_{a}=\frac{R_{a}}{R_{a}+R_{b}} V_{S}$

$$
V_{a}=\frac{1 \Omega}{1 \Omega+3 \Omega}(8 \mathrm{~V})=2 \mathrm{~V}
$$

What is the voltage drop across $R_{b}$ ?
$V_{b}=\frac{R_{b}}{R_{a}+R_{b}} V_{S} \quad V_{a}=\frac{3 \Omega}{1 \Omega+3 \Omega}(8 \mathrm{~V})=6 \mathrm{~V}$

## DC Voltage \& Current Sources

- An ideal DC voltage source outputs a constant voltage regardless of the amount of current through it.

- An ideal DC current source outputs a constant current regardless of the amount of voltage across it.



## Prefixes - common engineering style

- $10^{-9}$ nano $n$
- $10^{-6}$ micro m
- $10^{-3} \mathrm{milli}$
m
■ $10^{3}$ kilo k
- $10^{6}$ mega M
- $10^{9}$ giga $G$


## More circuit examples



## Find currents $\mathrm{i}_{1}$ and $\mathrm{i}_{2}$



## Find voltage v

Further questions:

1. Find the power in each resistor in the series and parallel examples.
2. Are household appliances connected in series or parallel? Why?
